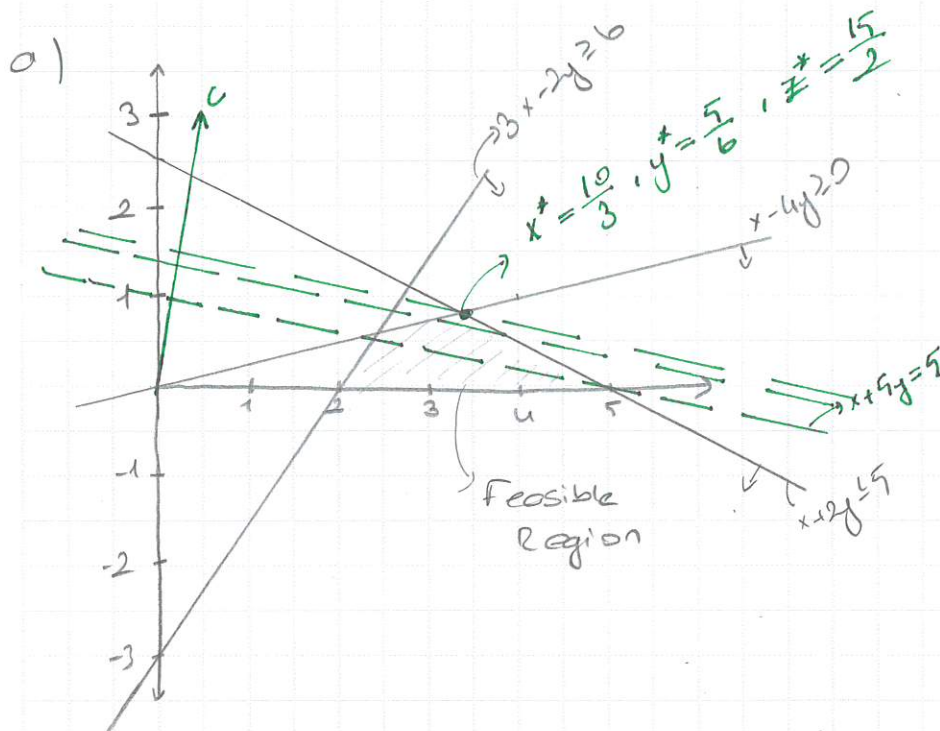


Question 1:

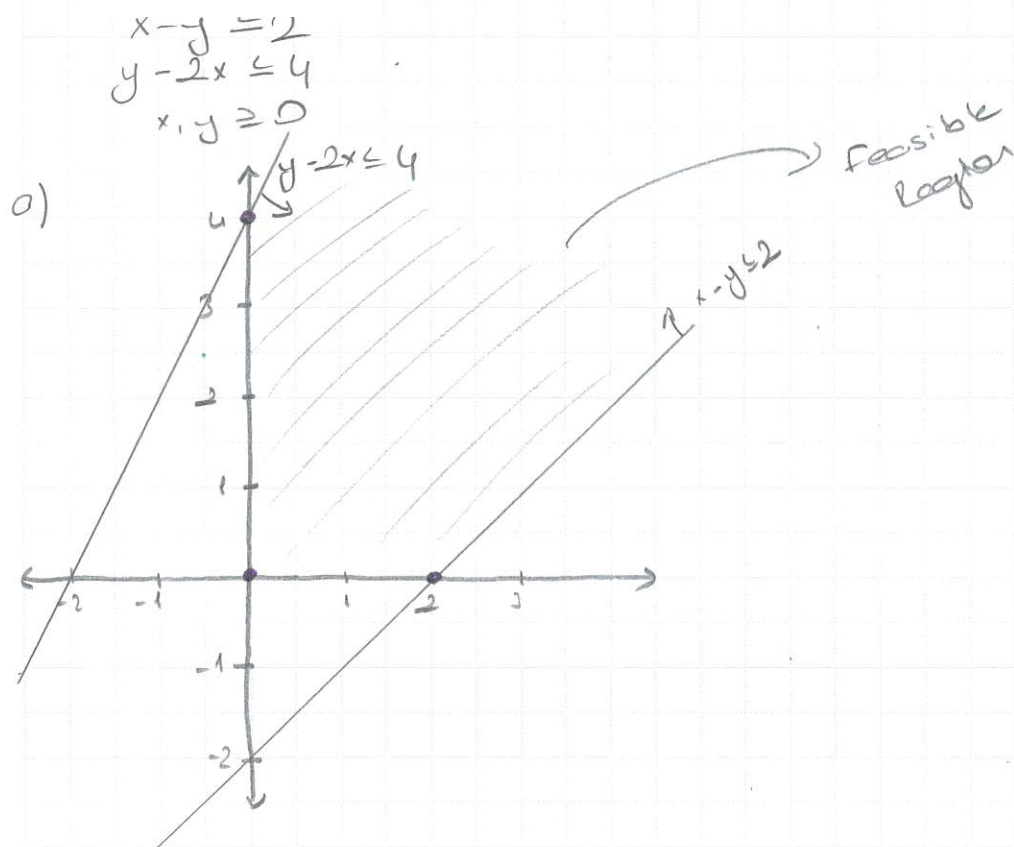
$$\begin{aligned} \max \quad & x + 5y \\ \text{s.t.} \quad & x + 2y \leq 5 \\ & 3x - 2y \geq 6 \\ & x - 4y \geq 0 \\ & x, y \geq 0 \end{aligned}$$



b) Optimal solution: $(x, y) = \left(\frac{10}{3}, \frac{5}{6}\right)$

Optimal objective function value: $z = x + 5y = \frac{15}{2}$

Question 2:



b) Since the only extremum points are $(0,4)$, $(0,0)$, $(2,0)$ we need to come up with obj. fens such that these points are uniquely optimal

e.g. Optimal soln: $(x,y) = (0,0)$

obj fen. $\rightarrow \min x+y \rightarrow$ opt. obj. fen. value: $= 0$,

Other possible solutions:

$$\begin{array}{ll}
 \max & -x - 3y \\
 \max & y - 3x \\
 \min & 5x + y
 \end{array}$$

c) We have 4 line segments, we need to come up with functions such that these line segments are optimal,

Possible solutions:

$$\begin{array}{ll} \max & x-y, \\ \min & y-x \end{array} \quad \begin{array}{l} z^* = (x-y) = 2 \\ z^* = (y-x) = -2 \end{array}$$

$$\begin{array}{ll} \max & y-2x \\ \min & 2x-y \end{array} \quad \begin{array}{l} z^* = (y-2x) = 4 \\ z^* = -4 \end{array}$$

$$\begin{array}{ll} \max & -x \\ \min & x \end{array} \quad z^* = 0$$

$$\begin{array}{ll} \min & y \\ \max & -y \end{array} \quad z^* = 0$$

d) Our objective function's improvement direction is towards the unbounded region.

e.g.

$$\begin{array}{ll} \min & -x-2y \\ \max & 3x-y \\ \min & -x-y \end{array}$$

e) Problem with a valid feasible region cannot be infeasible.

Question 3:

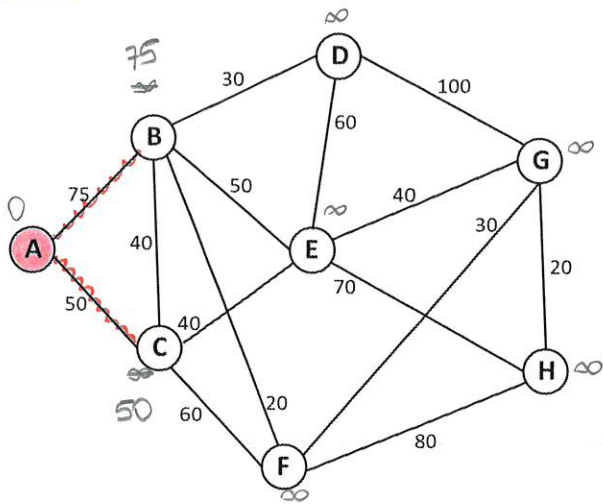
NN tour: From node S, nearest unvisited node is G. From node G, nearest unvisited node is F. From node F, nearest unvisited node is T. From node T, nearest unvisited node is E. All nodes are visited, we have to return to node S. Then the TSP tour with NN is SGFTES with cost:

$$(S \text{ to } G) + (G \text{ to } F) + (F \text{ to } T) + (T \text{ to } E) + (E \text{ to } S \text{ through } G \text{ without visiting } G) = (58) + (132) + (201) + (113) + (217 + 58) = 779.$$

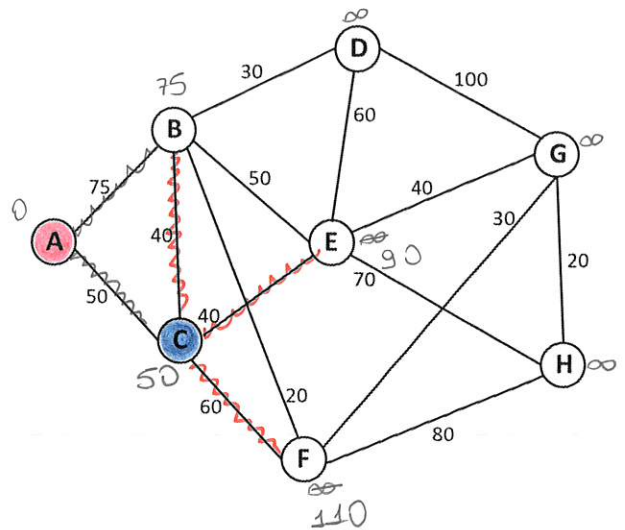
When we apply 2-opt, we switch GF and ES with GE and FS – as we do not want to have edges crossing each other. So the new TSP tour is SGETFS with cost $58 + 217 + 113 + 201 + 79 = 668$.

Question 4:

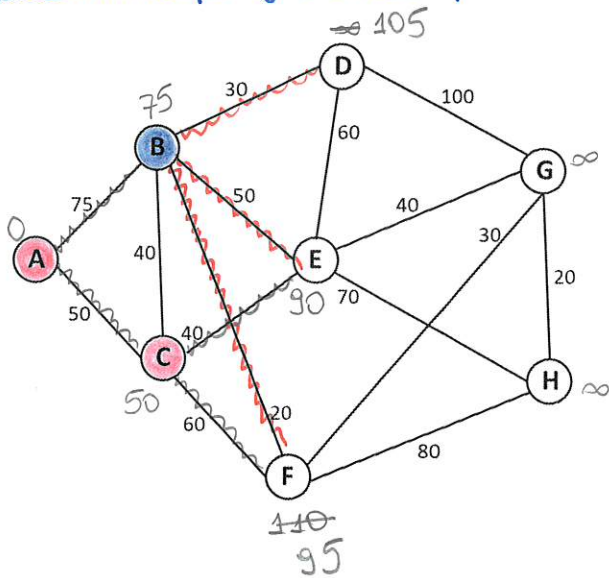
1) Initialize:



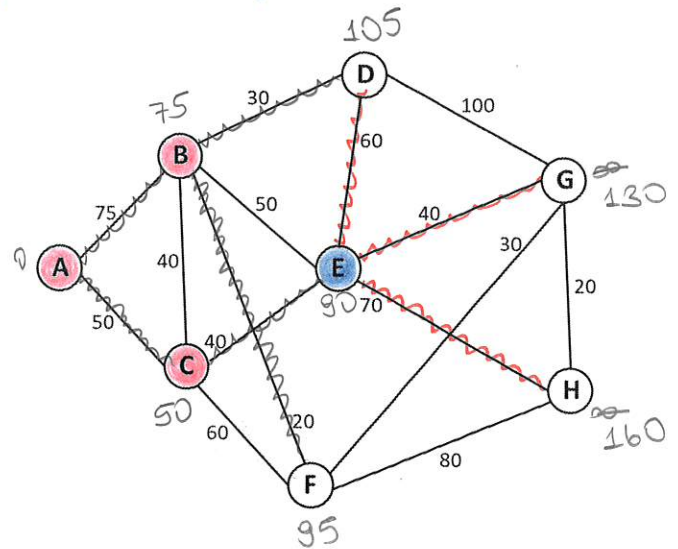
2) Choose min. temporary label and update:



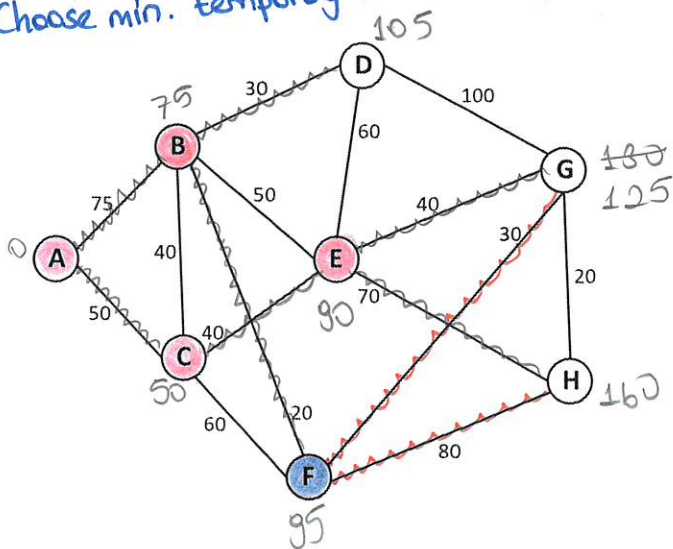
3) Choose min. temporary label and update:



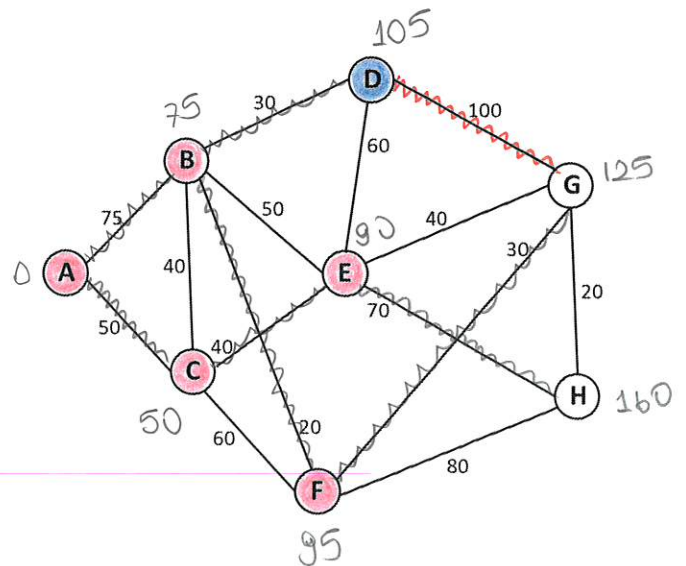
4) Choose min. temporary label and update:



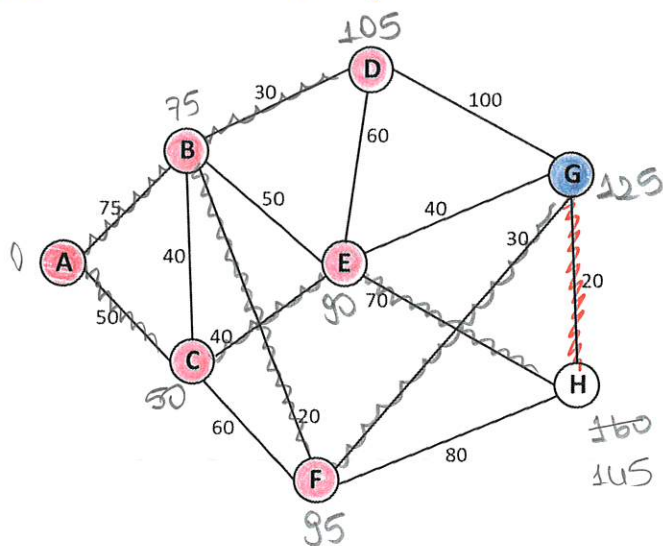
5) Choose min. temporary label and update:



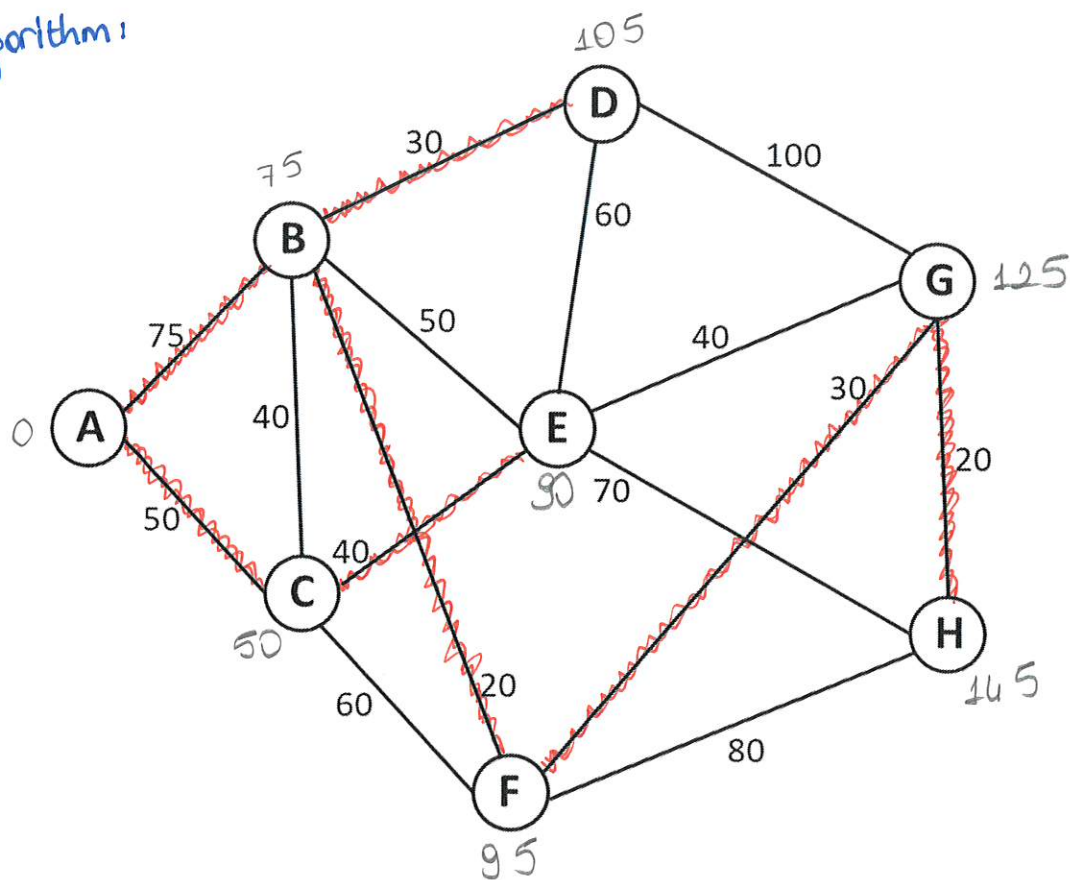
6) Choose min. temporary label and update:



7) Choose min. temporary label and update:



End of algorithm:



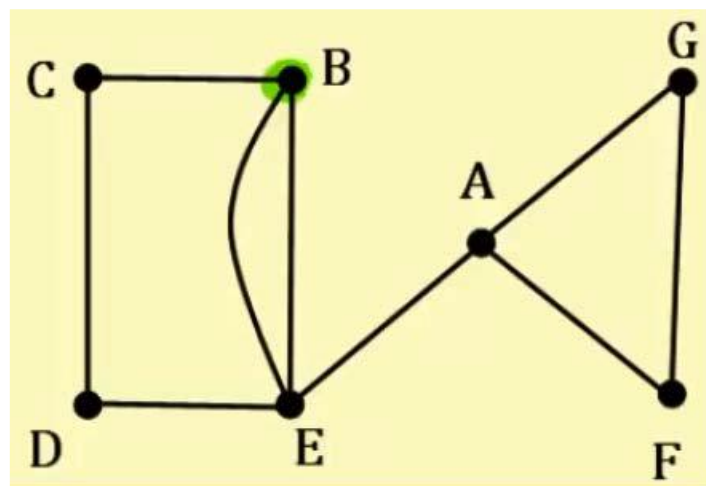
Shortest path from Node A to Node H: A B F G H

Distance: 145

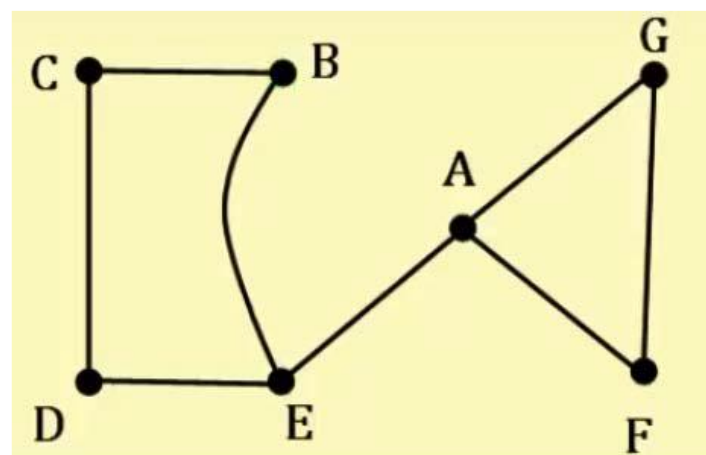
Question 5:

- a) You cannot form an Euler circuit/cycle using that network – Euler circuit/cycle requires you to form a tour starting and finishing at the same node visiting every edge – since there are four nodes with odd degree. The number of edges with odd degree should be exactly 0 to allow forming of an Euler circuit/cycle.
- b) Let's first look at the degrees of all vertices: A has a degree of 4, B has a degree of 4, C has a degree of 2, D has a degree of 2, E has a degree of 4, F has a degree of 2 and finally G has a degree of 2. So this graph allows us to form an Euler circuit/cycle as it is connected.

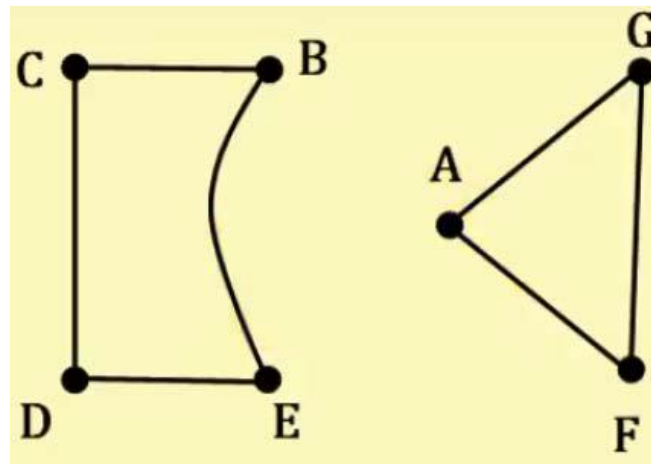
Let's start at vertex A. We have the freedom to choose edges AB, AC, AF and AG. Let's choose edge AB, circuit so far (csf) is AB.



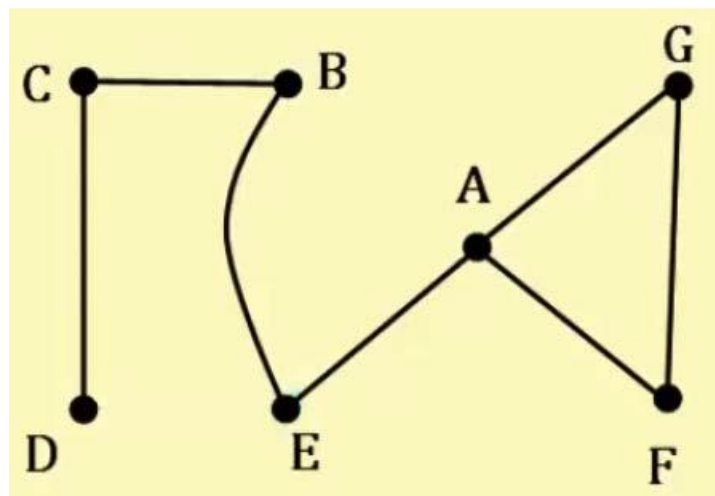
Edge AB is deleted. Now, let's choose edge BE and csf is ABE.



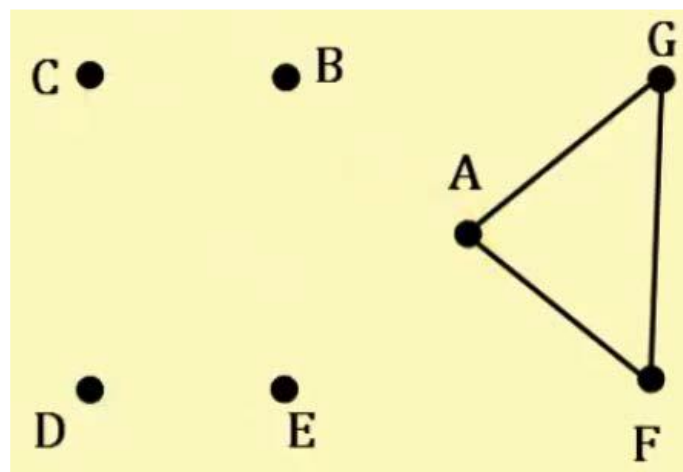
Edge BE is deleted. Now we need to be careful, if we choose edge EA, the graph will not be connected – there will be two disconnected graphs.



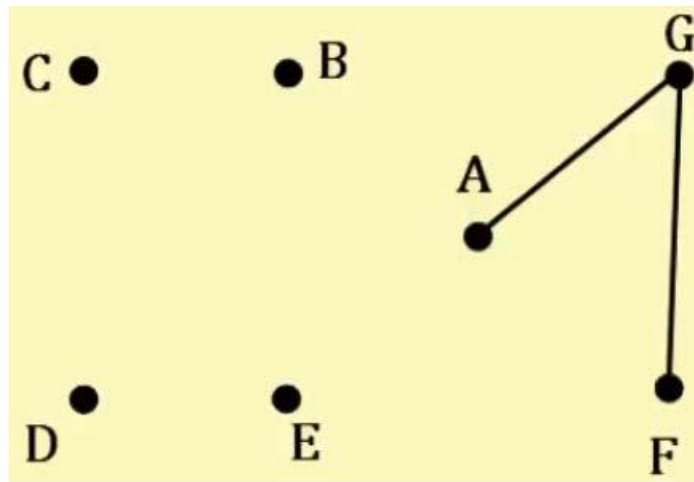
So, let's choose edge ED and csf is ABED.



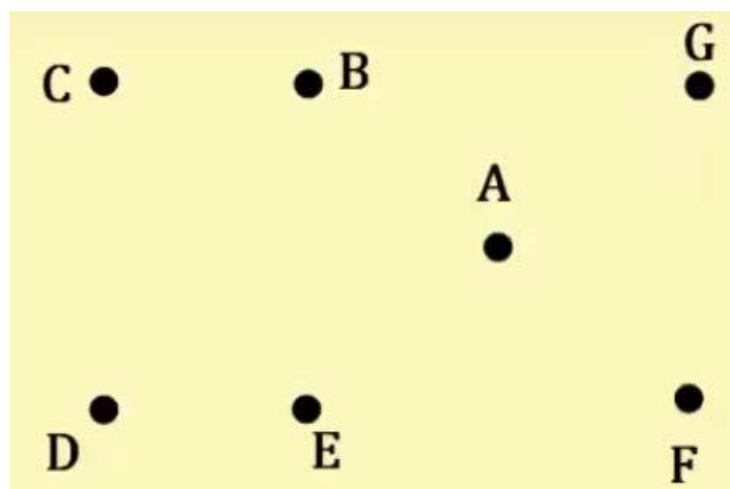
Remaining graph has one option for the next several choices, so let's skip those steps and have csf as ABEDCBEA.



Now, we can choose AF or AG. Let's choose AF and **csf** is ABEDCBEAF.



Again we have one option in each iteration from now on. So, **csf** is ABEDCBFAFGA.



Notice that all of the edges has been deleted, hence the Euler circuit is complete and it is ABEDCBFAFGA

Question 6:

a) Joey Crusher dominates Lenny Leonard.

Joey has more work experience and a higher CGPA.

All remaining attributes are the same.

That's why Joey will always be preferred over Lenny.

b) There are many ways to scale the criteria. The most basic one is to use the "best" and "worst" values of each criteria as its scale. However, for performance measures like CGPA, we know that there is already a preferred scale; then we could also make use of it in this context. A sample scale is shown below:

	Best	Worst		
Work Experience	8	0	→ max	} You might come up with a different scale (as long as you explain your reasoning)
CGPA	4.0	2.0	→ max	
WTW Night Shifts	Willing	Not Willing	→ max	
Salary Expectation	2800	3500	→ min	
Eagerness to work	Enthusiastic	Not motivated enough	→ max	

c) Normalise the values

Rating = $\frac{\text{Score} - \text{Worst}}{\text{Best} - \text{Worst}}$ → if max

Rating = $\frac{\text{Worst} - \text{Score}}{\text{Worst} - \text{Best}}$ → if min

	Work Exp.	CGPA	WTW Night Shifts	Salary Exp.	Eagerness to work
Herbert Powell	1	0.1	0	0	0
Lisa Simpson	0	0.7	0	1	1
Wayne Slater	0.75	0.6	1	0.14	0.5
Joey Crusher	0.5	0.5	0.5	0.71	0.5
Eugene Fisk	0.25	0.8	1	0.71	1

$$d) 0.2 + 0.25 + 0.15 = 0.6$$

Let w denote the weight for the "Eagerness to work" criterion.

Then $(0.4 - w)$ is the weight for "WTLW Night Shifts" criterion.

Using this substitution, we could calculate the overall scores of each candidate (in terms of w):

$$- \text{Herbert Powell: } 0.2 + (0.25)(0.01) = 0.2025$$

$$- \text{Lisa Simpson: } (0.7)(0.25) + (0.15)(1 + w) = 0.325 + w$$

$$- \text{Wayne Slater: } (0.75)(0.2) + (0.6)(0.25) + 1(0.4 - w) + (0.1w)(0.15) + 0.5w = 0.721 - 0.5w$$

$$- \text{Joey Crusher: } (0.5)(0.2) + (0.5)(0.25) + (0.5)(0.4 - w) + (0.7)(0.15) + 0.5w = 0.5315$$

$$- \text{Eugene Fisk: } (0.25)(0.2) + (0.8)(0.25) + 1(0.4 - w) + (0.7)(0.15) + 1w = 0.7565$$

We know that $w \geq 0$, therefore $0 \leq w \leq 0.4$.

- 3 of the candidates have overall scores independent from w : Herbert, Joey, Eugene.

No candidate could reach 0.7565 even the w is 0.4.

Therefore Eugene Fisk is the candidate to hire no matter what the w value is.

Question 7:

- a) First constraint is for relating production rates with total available hours for production. We cannot use more than the given time.

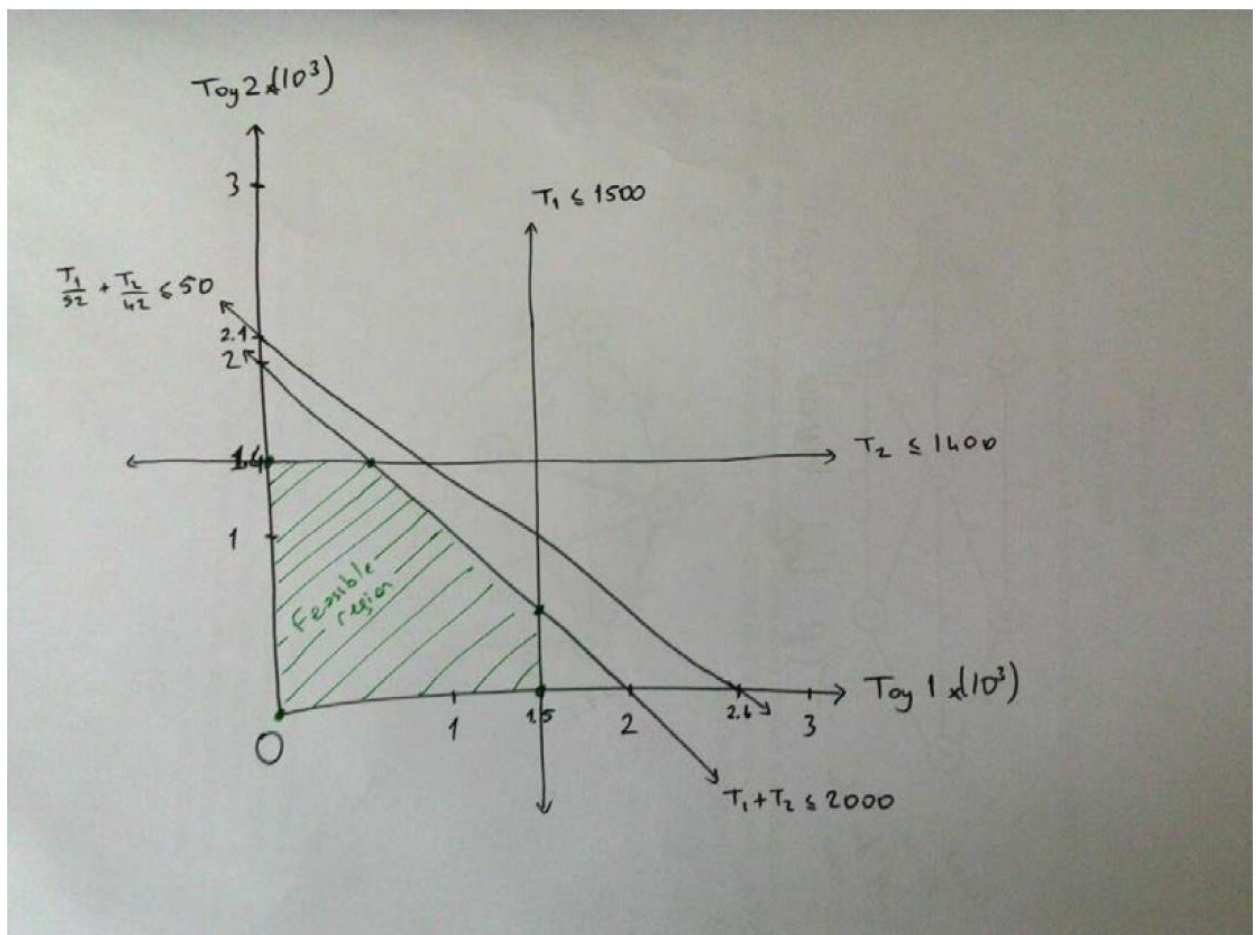
Second constraint is for market research which says that at most 2000 toys can be sold combined.

Third constraint is for maximum demand of Toy1, which is 1500.

Fourth constraint is for maximum demand of Toy2, which is 1400.

Fifth and the constraint is non-negativity (integrality) constraint. It denotes that the produced amounts for each type of toy cannot be nonnegative.

- b) A correction here, let's use the right hand side of first constraint as 50 rather than 420, for scaling reasons. And let's denote the axes as to the power of 10 to the 3, just to have a better visualization.



The objective function is $12T_1 + 16T_2$, so if we put the isoprofit line onto the graph, we obtain (600, 1400) as our optimal solution. And the total profit is \$29,600.

Question 8:

a)

	a	b	c	d	e	f
a	-	1	4	4	7	3
b	1	-	3	3	6	2
c	4	3	-	2	4	3
d	4	3	2	-	3	1
e	7	6	4	3	-	4
f	3	2	3	1	4	-

b) There are $\binom{6}{2} = 15$ combinations. List all combinations and respective travel times to reach each district.

	ab	ac	ad	ae	af	bc	bd	be	bf	cd	ce	cf	de	df	ef
a	0	0	0	0	0	1	1	1	1	4	4	3	4	3	3
b	0	1	1	1	1	0	0	0	0	3	3	2	3	2	2
c	3	0	2	4	3	0	2	3	3	0	0	0	2	2	3
d	3	2	0	3	1	2	0	3	1	0	2	1	0	0	1
e	6	4	3	0	4	4	3	0	4	3	0	4	0	3	0
f	2	3	1	3	0	2	1	2	0	1	3	0	1	0	0
TOTAL TIME	14	10	7	11	9	9	7	9	9	11	12	10	10	10	9

If total sum of time reaching every district is minimized, ad OR bd should be selected as fire stations location combinations.

c) To cover every district in shortest possible time, the worst time accessing a district should be minimum. Therefore, we should focus on column (or row) maximums to find the worst time for accessing a district from an open facility.

From a : 7 (to e)

From b : 6 (to e)

From c : 4 (to a or e)

From d : 4 (to a)

From e : 7 (to a)

From f : 4 (to f)

The fire station should be located at C OR D OR F in order to obtain minimum coverage time (which is 4).

d) Construct 0/1 coverage matrix for $\delta = 3$.

If time $> 3 \Rightarrow 0$.
time $\leq 3 \Rightarrow 1$.

	a	b	c	d	e	f
a	1	1	0	0	0	1
b	1	1	1	1	0	1
c	0	1	1	1	0	1
d	0	1	1	1	1	1
e	0	0	0	1	1	0
f	1	1	1	1	0	1

i) The locations that satisfy full coverage of the city are:

ad, bd, be, df, ef. (when you sum up the rows or columns in opt matrix for these combinations, all entries are at least 1.)

ii)

	ad	bd	be	df	ef
Sum of time reaching each district	7	7	9	10	9
Worst time for reaching a district	3	2	3	3	3
Number of times covered districts	2	4	1	4	1

iii)

	Best	Worst	
Scale of criterion 1:	7	10	→ To be minimized
Scale of criterion 2:	2	3	→ To be minimized
Scale of criterion 3:	4	1	→ To be maximized

To normalize the ratings apply the following formulas:

$$\text{Rating} = \frac{\text{Score} - \text{Worst}}{\text{Best} - \text{Worst}} \quad (\text{if max})$$

$$\text{Rating} = \frac{\text{Worst} - \text{Score}}{\text{Worst} - \text{Best}} \quad (\text{if min})$$

	ad	bd	be	df	ef
Crit 1	1	1	0.67	0	0.67
Crit 2	0	1	0	0	0
Crit 3	0.34	1	0	1	0

The results are rounded to the nearest 2 decimals.

iv) bd has 1's all over its column, that's why we could infer that it is the best combination without making any computations. To rank the others, let's make the necessary computations.

$$\text{Score}(ad) = 1 \cdot 0,2 + 0 + 0,34 \cdot 0,5 = 0,37$$

$$\text{Score}(bd) = 1 \cdot 0,2 + 1 \cdot 0,3 + 1 \cdot 0,5 = 1$$

$$\text{Score}(be) = 0,67 \cdot 0,2 + 0 + 0 = 0,134$$

$$\text{Score}(df) = 0 + 0 + 1 \cdot 0,5 = 0,5$$

$$\text{Score}(ef) = 0,67 \cdot 0,2 + 0 + 0 = 0,134$$

Then the preference order is:

$$bd \succ df \succ ad \succ be \sim ef$$

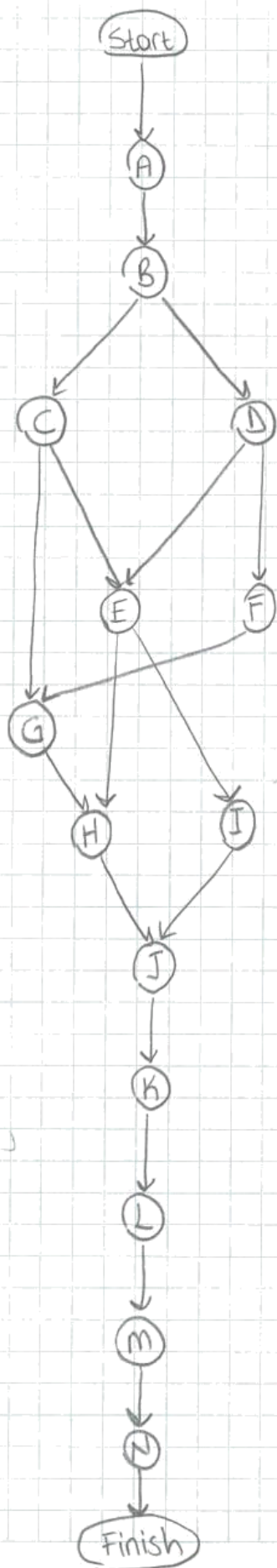
Remark: " $\succ$ " is the preference operator.

$x \succ y$ denotes that x is strongly preferred over y .

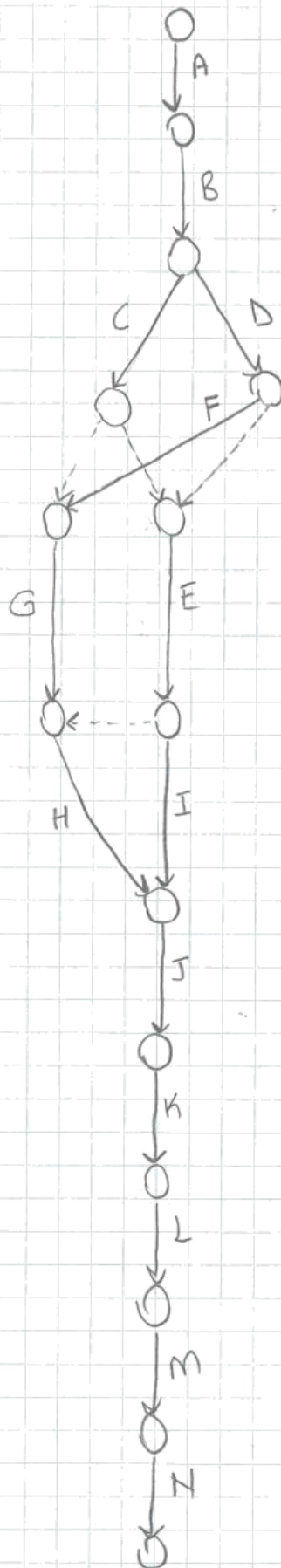
Similarly, " $\sim$ " shows the indifference between two options.

Question 9:

a) AON network:



b) AOA network:



c) 2 d)

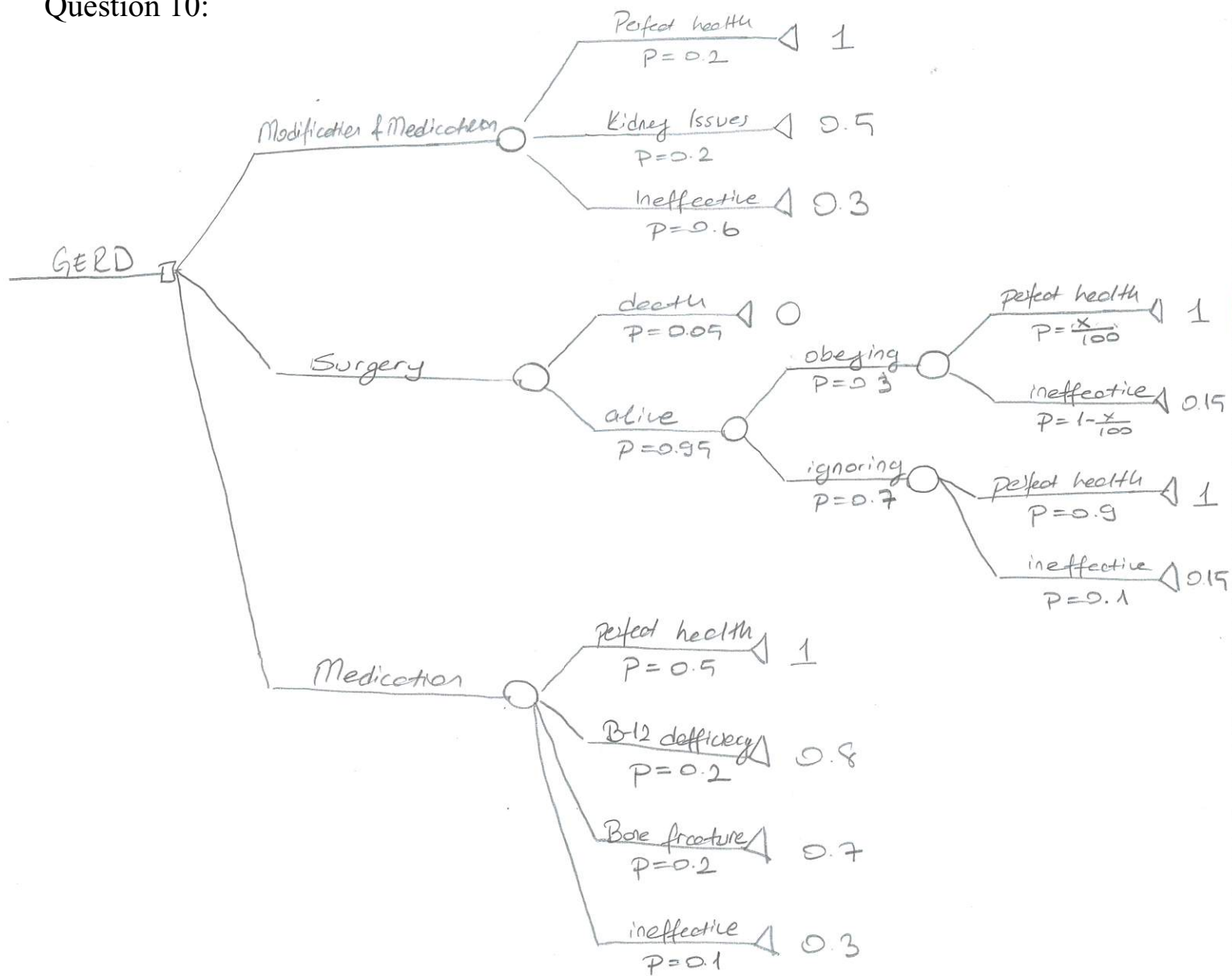
Activity	ES	EF	LS	LF	Stock	On Critical Path?
A	0	5	0	5	0	YES
B	5	8	5	8	0	YES
C	8	10	20	22	12	NO
D	8	12	8	12	0	YES
E	12	20	22	30	10	NO
F	12	24	12	26	0	YES
G	24	30	26	30	0	YES
H	30	34	30	34	0	YES
I	20	22	32	34	12	NO
J	34	39	34	39	0	YES
K	39	42	39	42	0	YES
L	42	43	42	43	0	YES
M	43	46	43	46	0	YES
N	46	48	46	48	0	YES

e) Critical Path:

A, B, D, F, G, H, J, K, L, M, N

Completion Time = 48 days

Question 10:



Expected utility of life-style modification and over-the-counter medications:

$$:= 1 \cdot (0.2) + 0.5 \cdot (0.2) + 0.3 \cdot (0.6)$$

$$= 0.48$$

Expected utility of surgery

$$:= 0 \cdot (0.05) + 0.95 \left(0.3 \left(\frac{x}{100} + \left(1 - \frac{x}{100} \right) \cdot 0.15 \right) + 0.7 \left(0.9 + 0.1 \cdot 0.15 \right) \right)$$

$$= 0.684 + 0.243 \cdot \frac{x}{100}$$

Expected utility of prescription medication

$$\begin{aligned} &= 1(0.5) + 0.8(0.2) + 0.7(0.2) + 0.3(0.1) \\ &= 0.83 \end{aligned}$$

In order surgery to be chosen, expected utility of it should be higher than the remaining options.

$$(1) \quad 0.684 + 0.243 \cdot \frac{x}{100} > 0.48$$

$$(2) \quad 0.684 + 0.243 \cdot \frac{x}{100} > 0.83$$

(2) is a tighter inequality, therefore,

from (2) $x > 60.08$, let's say x should be at least 61

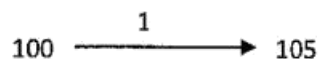
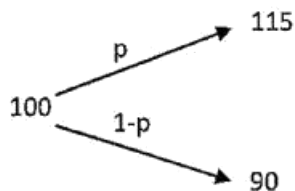
Expected utility of surgery when $x=61$

we plug $x=61$ to the equation,

$$0.684 + 0.243 \cdot \frac{61}{100} = 0.832$$

Question 11:

i)



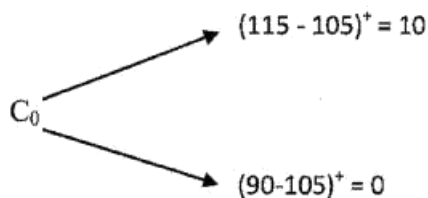
a) $u = 115/100 = 1.15$

$d = 90/100 = 0.9$

$1+r = 105/100 = 1.05, r = 0.05$

b) $d - 1 = -0.1 < r = 0.05 < u - 1 = 0.15$. By the fundamental theorem of asset pricing, we conclude that the model satisfies the principle of no-arbitrage.

c) The payoff price tree for the call is as follows:

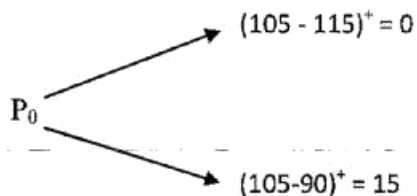


Let (x,y) be a replicating strategy. It satisfies the system.

$$\begin{cases} 115x + 105y = 10 \\ 90x + 105y = 0 \end{cases} \quad 25x = 10, x = \frac{2}{5} \text{ \& } y = -\frac{12}{35}$$

Hence the call price is $C_0 = 100x + 100y = 40/7$.

d) The payoff price tree is as follows:



Let (x,y) be a replicating strategy. It satisfies the system.

$$\begin{cases} 115x + 105y = 0 \\ 90x + 105y = 15 \end{cases} \quad 25x = -15, x = -\frac{3}{5} \text{ \& } y = \frac{23}{35}$$

Hence the price is $P_0 = 100x + 100y = 40/7$.

e)

$$115x + 105y = 115 - F \quad (1)$$

$$90x + 105y = 90 - F \quad (2)$$

$$100x + 100y = 0, y = -x$$

$$\left. \begin{array}{l} (1) 115x - 105x = 10x = 115 - F \\ (2) 90x - 105x = -15x = 90 - F \end{array} \right\} -\frac{2}{3} = \frac{115 - F}{90 - F}, F = 105 = 100(1 + 0.05)$$

ii)



a) $u = 99/90 = 1.1$

$d = 81/90 = 0.9$

$1+r = 95/100 = 0.95, r = -0.05$

b) $d - 1 = -0.1 < r = -0.05 < u - 1 = 0.1$. By the fundamental theorem of asset pricing, we conclude that the model satisfies the principle of no-arbitrage.

c) The payoff price tree for the call is as follows:

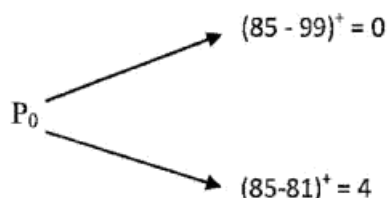


Let (x, y) be a replicating strategy. It satisfies the system.

$$\left. \begin{array}{l} 99x + 95y = 14 \\ 81x + 95y = 0 \end{array} \right\} 18x = 14, x = \frac{7}{9} \text{ \& } y = -\frac{63}{95}$$

Hence the call price is $C_0 = 90x + 100y = 70/19$.

d) The payoff price tree is as follows:



Let (x,y) be a replicating strategy. It satisfies the system.

$$\begin{cases} 99x + 95y = 0 \\ 81x + 95y = 4 \end{cases} \quad 18x = -4, x = -\frac{2}{9} \text{ \& } y = \frac{22}{95}$$

Hence the price is $P_0 = 100x + 100y = 60/19$.

e)

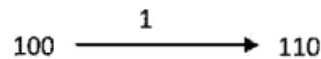
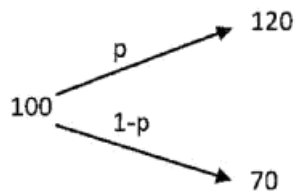
$$99x + 95y = 99 - F \quad (1)$$

$$81x + 95y = 81 - F \quad (2)$$

$$90x + 100y = 0, x = -10y/9$$

$$\begin{cases} (1) - 110y + 95y = -15y = 99 - F \\ (2) - 90y + 95y = 5y = 81 - F \end{cases} \quad -3 = \frac{99 - F}{81 - F}, F = 85.5 = 90(1 - 0.05)$$

iii)



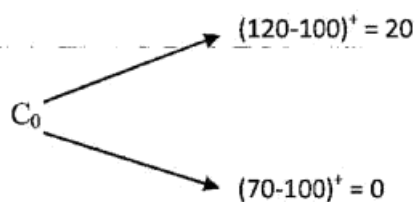
$$a) u = 120/100 = 1.2$$

$$d = 70/100 = 0.7$$

$$1+r = 110/100 = 1.10, r = 0.1$$

b) $d - 1 = -0.3 < r = 0.1 < u - 1 = 0.2$. By the fundamental theorem of asset pricing, we conclude that the model satisfies the principle of no-arbitrage.

c) The payoff price tree for the call is as follows:

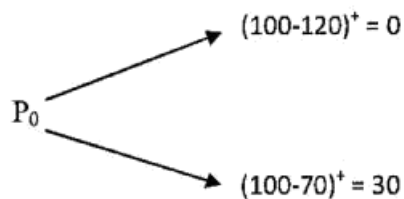


Let (x,y) be a replicating strategy. It satisfies the system.

$$\begin{cases} 120x + 110y = 20 \\ 70x + 110y = 0 \end{cases} \Rightarrow 50x = 20, x = \frac{2}{5} \& y = -\frac{14}{55}$$

Hence the call price is $C_0 = 100x + 100y = 160/11$.

d) The payoff price tree is as follows:



Let (x,y) be a replicating strategy. It satisfies the system.

$$\begin{cases} 120x + 110y = 0 \\ 70x + 110y = 30 \end{cases} \Rightarrow 50x = -30, x = -\frac{3}{5} \& y = \frac{36}{55}$$

Hence the price is $P_0 = 100x + 100y = 60/11$.

e)

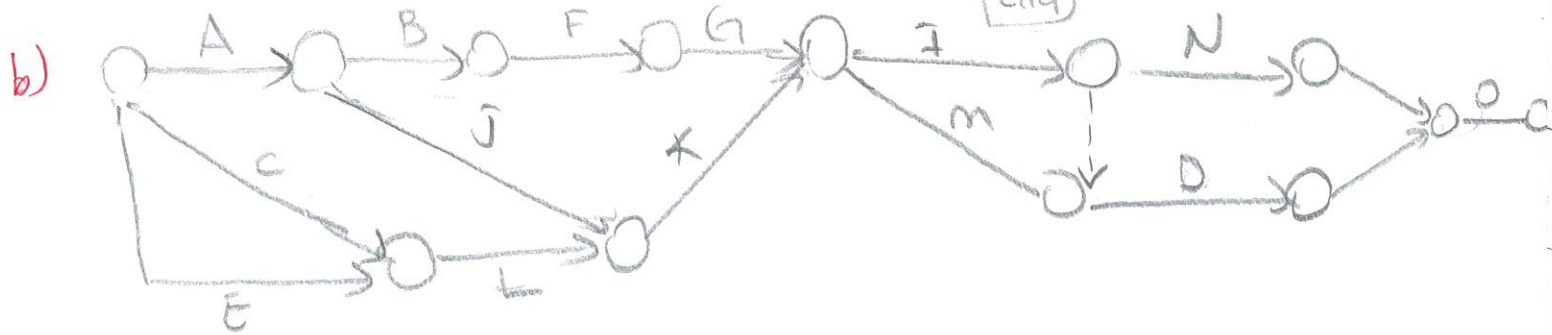
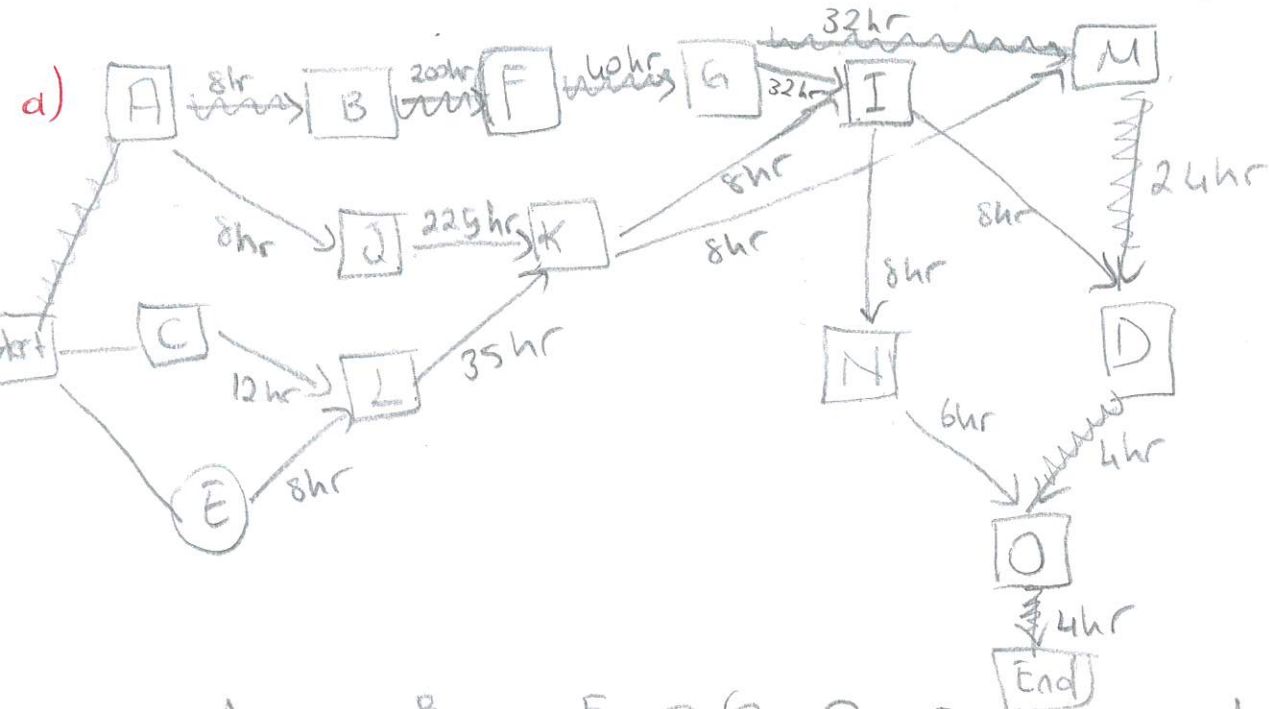
$$120x + 110y = 120 - F \quad (1)$$

$$70x + 110y = 70 - F \quad (2)$$

$$100x + 100y = 0, y = -x$$

$$\begin{cases} (1) 120x - 110x = 10x = 120 - F \\ (2) 70x - 110x = -40x = 70 - F \end{cases} \Rightarrow -\frac{1}{4} = \frac{120 - F}{70 - F}, F = 110 = 100(1 + 0.1)$$

Question 12:



c)

Activity	ES	EF	LS	LF	Slack
A	0	8	0	8	0
B	8	208	8	208	0
C	0	12	225	237	225
D	304	308	304	308	0
E	0	8	229	237	229
F	208	248	208	248	0
G	248	280	248	280	0
H	280	288	294	302	14
I	280	288	294	302	14
J	8	233	47	292	39
K	233	241	272	280	39
L	12	47	237	272	225
M	280	304	280	304	0
N	288	294	302	308	14
O	308	312	308	312	0

e) Completion time = 312 hr Critical path = A B F G M O O

Question 13

a)

	A	B	C	D	E	F	G	H	I
A	0	3	5	4	8	13	10	14	13
B	3	0	2	3	6	14	12	11	16
C	5	2	0	1	4	12	7	17	10
D	4	3	1	0	5	11	6	13	9
E	8	6	4	5	0	11	6	13	9
F	13	14	12	11	11	0	5	12	7
G	10	12	7	6	6	5	0	7	3
H	14	11	17	13	13	12	7	0	9
I	13	16	10	9	9	7	3	9	0

b)

	AB	AC	AD	AE	AF	AG	AH	AI	BC	BD	BE	BF	BG	BH	BI	CD	CE	CF	CG	CH	CI	DE	DF	DG	DH	DI	EF	EG	EH	EI	FG	FH	FI	GH	GI	HI
A	0	0	0	0	0	0	0	0	3	3	3	3	3	3	3	4	5	5	5	5	5	4	4	4	4	4	8	8	8	8	10	13	13	10	10	13
B	0	2	3	3	3	3	3	3	0	0	0	0	0	0	0	2	2	2	2	2	2	3	3	3	3	3	6	6	6	6	12	11	14	11	12	11
C	2	0	1	4	5	5	5	5	0	1	2	2	2	2	2	0	0	0	0	0	0	1	1	1	1	1	4	4	4	4	7	12	10	7	7	10
D	3	1	0	4	4	4	4	4	1	0	3	3	3	3	3	0	1	1	1	1	1	0	0	0	0	0	5	5	5	5	6	11	9	6	6	9
E	6	4	5	0	8	6	8	8	4	5	0	6	6	6	6	4	0	4	4	4	4	0	5	5	5	5	0	0	0	0	6	11	9	6	6	9
F	13	12	11	11	0	5	12	7	12	11	11	0	5	12	7	11	11	0	5	12	7	11	0	5	11	7	0	5	11	7	0	0	0	5	5	7
G	10	7	6	6	5	0	7	3	7	6	6	5	0	7	3	6	6	5	0	7	3	6	5	0	6	3	5	0	6	3	0	5	3	0	0	3
H	11	14	13	13	12	7	0	9	11	11	11	11	7	0	9	13	13	12	7	0	9	13	12	7	0	9	12	7	0	9	7	0	9	0	7	0
I	13	10	9	9	7	3	9	0	10	9	9	7	3	9	0	9	9	7	3	9	0	9	7	3	9	0	7	3	9	0	3	7	0	3	0	0
	58	50	48	50	44	33	48	39	48	46	45	37	29	42	33	49	47	36	27	40	31	47	37	28	39	32	47	38	49	42	51	70	67	48	53	62

c)

from	A	14	to	H
from	B	16	to	I
from	C	17	to	H
from	D	13	to	H
from	E	13	to	H
from	F	14	to	B
from	G	12	to	B
from	H	17	to	C
from	I	16	to	B

d)

Coverage Matrix

	A	B	C	D	E	F	G	H	I
A		1	1	1	1	0	0	0	0
B		1	1	1	1	1	0	0	0
C		1	1	1	1	1	0	1	0
D		1	1	1	1	1	0	1	0
E		0	1	1	1	1	0	1	0
F		0	0	0	0	0	1	1	0
G		0	0	1	1	1	1	1	1
H		0	0	0	0	0	0	1	1
I		0	0	0	0	0	1	1	0

i)

	AB	AC	AD	AE	AF	AG	AH	AI	BC	BD	BE	BF	BG	BH	BI	CD	CE	CF	CG	CH	CI	DE	DF	DG	DH	DI	EF	EG	EH	EI	FG	FH	FI	GH	GI	HI
A	2	2	2	1	1	1	1	1	2	2	1	1	1	1	1	2	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0
B	2	2	2	2	1	1	1	1	2	2	2	1	1	1	1	2	2	1	1	1	1	2	1	1	1	1	1	1	1	1	0	0	0	0	0	0
C	2	2	2	2	1	2	1	1	2	2	2	1	2	1	1	2	2	1	2	1	1	2	1	2	1	1	1	2	1	1	1	0	0	1	1	0
D	2	2	2	2	1	2	1	1	2	2	2	1	2	1	1	2	2	1	2	1	1	2	1	2	1	1	1	2	1	1	1	0	0	1	1	0
E	1	1	1	1	0	1	0	0	2	2	2	1	2	1	1	2	2	1	2	1	1	2	1	2	1	1	1	2	1	1	1	0	0	1	1	0
F	0	0	0	0	1	1	0	1	0	0	0	1	1	0	1	0	0	1	1	0	1	0	1	1	0	1	1	1	0	1	2	1	2	1	2	1
G	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2
H	0	0	0	0	0	1	1	0	0	0	0	0	1	1	0	0	0	0	1	1	0	0	0	1	1	0	0	1	1	0	1	1	0	2	1	1
I	0	0	0	0	1	1	0	1	0	0	0	1	1	0	1	0	0	1	1	0	1	0	1	1	0	1	1	1	0	1	2	1	2	1	2	1

ii)

	AG	BG	CG	DG
The total Distance	33	29	27	28
number of twice coverage	2	3	4	3

	Best	Worst	
scale of criteria 1	27	33	to minimize
scale of criteria 2	4	2	to maximize

iii)

	AG	BG	CG	DG	weight
c1	0	0.666667	1	0.833333	0.6
c2	0	0.5	1	0.5	0.4

iv)

Alternatives	AG	BG	CG	DG
Total Score	0	0.6	1	0.7