

HW 3 ANSWERS

1A)

1. We have identical 52 shipments.

$$Q = \lambda / 52$$

$$AC(1) = (A + K) * 52 \text{ if } k \geq \lambda / 52$$

$$AC(1) = (m_1 * A + K) * 52 \text{ where } m_1 = \lfloor \lambda / 52k \rfloor \text{ if } k < \lambda / 52$$

2. We have $Q = C$ and $\lfloor \lambda / C \rfloor$ shipments.

$$AC(2) = (A + K) * \lfloor \lambda / C \rfloor \text{ if } k \geq C$$

$$AC(2) = (m_2 * A + K) * \lfloor \lambda / C \rfloor \text{ where } m_2 = \lfloor C / k \rfloor \text{ if } k < C$$

3. We have $Q = 3C$ and $\lfloor \lambda / 3C \rfloor$ shipments.

$$AC(3) = (A + K) * \lfloor \lambda / 3C \rfloor \text{ if } k \geq 3C$$

$$AC(3) = (m_3 * A + K) * \lfloor \lambda / 3C \rfloor \text{ where } m_3 = \lfloor 3C / k \rfloor \text{ if } k < 3C$$

1B)

$\lambda = 720$ units, $K = \$160$, $A = \$300$, $C = 40$ units; k can take two values - $k = 120$ or 25 .

$$\text{Policy 1: } Q = 720 / 52 = 13.85$$

When $k = 120$ or 25 , $k > Q$

$$AC(1) = (A + K) * 52 = (300 + 160) * 52 = \$23920$$

$$\text{Policy 2: } k = 120 \geq 40 = C$$

$$AC(2) = (A+K) * [\lambda / C] = (300+160) * [720 / 40] = \$8280$$

$$k = 25 < 40 = C$$

$$AC(2) = (m_2 * A + K) * [\lambda / C] = ([40 / 25] * 300 + 160) * 18 = \$8280$$

Policy 3:

$$k = 120 = 3C = 120$$

$$AC(3) = (A+K) * [\lambda / 3C] = (300+160) * [720 / 120] = 2760$$

$$k = 25 < 3C = 120$$

$$AC(3) = (m_3 * A + K) * [\lambda / 3C] = (4 * 300 + 160) * [720 / 120] = 8160$$

Policy 1 gives the worst cost for both k values and Policy 3 gives the minimum cost for both k values.

1C) Holding cost issue, storage space limitation can be problematic despite low annual costs of policies.

$$2) \lambda = 20 \text{ cars/day} = 20 * 360 = 7200 \text{ cars/year}$$

$$c = 1500 \text{ TL}$$

$$h = 22 \% * c = 330 \text{ TL/ unit/ year}$$

$$K = 13000 \text{ TL}$$

$$L = 20 \text{ days} = 1/18 \text{ year}$$

$$1 \text{ year} = 360 \text{ days}$$

$$2A) Q^* = EOQ = \sqrt{2K\lambda/h} = 753.18$$

$$2B) \frac{K\lambda}{Q} + \frac{hQ}{2} = 248547.78 \text{ TL}$$

$$2C) T = Q/\lambda = 0.1 \text{ year or 36 days}$$

2D) $R = \lambda * L = 20 \text{ cars/day} * 20 \text{ days} = 400 \text{ cars}$ (Reorder point is the inventory level at which you will order so that new order arrives at the instant your inventory level goes to zero.

2E) Let x be the the first time the manufacturer should place an order to its engine supplier in Japan. $I_0 = 1200$, $R = 400$ and $L = 20$ days. Thus,

$$\frac{x}{x+L} = \frac{I_0-R}{I_0}, \text{ and } x = 40^{\text{th}} \text{ day.}$$

2F)

- i) Due to the convexity of the average annual function, manufacturer would choose 75% of the quantity in 2A) = $753.18 * 0.75 = 564.89 = Q$
- ii) $\frac{K\lambda}{Q} + \frac{hQ}{2} = 258902.83 \text{ TL}$. Capacity constraint added 10355.05 TL to the annual cost.

